

1 **Comparison of the ranges of uncertainty captured in different seismic hazard studies**

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21 INTRODUCTION

22
23 The inclusion of epistemic uncertainties, generally via logic trees (Kulkarni et al., 1984), within
24 probabilistic seismic hazard assessments (PSHAs) is becoming standard for all types of studies
25 (commercial, governmental or research; site-specific, national, regional or global). Consequently
26 many studies publish expected ground motions for a given annual frequency of exceedance
27 (AFE) or return period derived from the hazard curves for the mean, median and various fractiles
28 (percentiles). The spread of these values represents the uncertainty captured in the results (the
29 greater the spread the higher the uncertainty). For example, Figure 1 shows the distribution of
30 AFE for a peak ground acceleration (PGA) of 0.25g obtained in the study for the WNP-2 nuclear
31 power plant (Hanford Reservation, Washington State) reported by Kulkarni et al. (1984).
32 Distributions of ground-motion levels for a given AFE are now most commonly reported in
33 recent PSHAs rather than distributions of AFEs for a certain ground-motion level.

34
35 Woo (2002) calls for the epistemic uncertainty to be overlaid on seismic hazard maps, although
36 this is rarely if ever done. Giardini et al. (2004, their Figure 34) present the relative uncertainty in
37 the Swiss national seismic hazard map showing that parts of the map are associated with
38 considerable uncertainty (more than 40%) because of doubts over the seismic source zones and b-
39 values. A recent detailed study of epistemic uncertainties in a PSHA is by Bradley et al. (2012),
40 who rank the impact of various uncertainties on hazard results for two New Zealand cities
41 (Wellington and Christchurch). There are, however, no studies to our knowledge where these
42 distributions are compared *among* PSHAs. As we seek to show in this brief article, such
43 comparisons can provide useful insights into the suitability of the distributions of the input

44 parameters within the logic trees. For example, if the range of uncertainty of a study is much
45 narrower than the uncertainty present in comparable PSHAs for a similar location then it could
46 indicate that the uncertainties in the input parameters (e.g. seismic source characterization) have
47 not been completely captured. Additional data collection and analysis can significantly reduce
48 epistemic uncertainty and this should be done when possible — all remaining uncertainties
49 should be accounted for within the final PSHA.

50

51 **SELECTED STUDIES AND UNCERTAINTY MEASURES**

52

53 In this study we consider various published PSHAs for rock sites that report expected PGAs and
54 (pseudo)-spectral accelerations (PSAs) for a structural period of 1s and 5% of critical damping
55 for: the mean¹, median (50th percentile) and 15th (or 16th) and 85th (or 84th) percentiles for return
56 periods of 475 (10% chance of exceedance in 50 years, AFE of $1/475=2.1 \times 10^{-3}$) and 2 475 years
57 (2% chance of exceedance in 50 years, AFE of $1/2475=4.0 \times 10^{-4}$). Examining the relationships
58 between these ground-motion levels will allow an assessment of the reported uncertainty in the
59 hazard results to be made. These ground-motion measures and AFEs were considered because
60 they are the results most commonly reported in PSHAs for standard infrastructure. For facilities
61 such as nuclear power plants, lower AFEs (or longer return periods) and a wider range of
62 percentiles (e.g. 5 and 95th) are often published but these are not considered here. The only
63 component of the PSHA that differs when considering PGA, PSA(1s) or PSA at another
64 structural period is the intensity measure (IM) for which the ground motion prediction equations

¹ Bommer and Scherbaum (2008) note that the two methods to compute this parameter (either calculation of the mean ground motion at each AFE or, correctly, that based on statistics of the AFEs for each ground-motion amplitude) can lead to different results. Here we simply use the values reported by the authors irrespective of which method they use, which is very rarely stated.

65 (GMPEs) are evaluated. Douglas (2010) shows that the epistemic uncertainty associated with
66 GMPEs are comparable for PSA (considering a natural period of 1s as an example) and PGA.
67 Long-period PSAs can, however, be more sensitive to uncertainties in the recurrence rates of
68 large earthquakes (e.g. through the M_{\max} used in the magnitude-frequency relations) than short-
69 period intensity measures, such as PGA (Julian Bommer, written communication, 2014). Hence,
70 the period-dependency of the uncertainty is examined here.

71
72 The PSHAs selected comprise various regional, national or site-specific studies where the
73 required information for such a comparison is freely available from published hazard curves,
74 which may have required digitization or interpolation, or tables. Despite using detailed logic trees
75 the hazard results of the US National Seismic Hazard Mapping Project (e.g. Petersen et al., 2008)
76 are only published for the mean ground motion and hence this study is not included here. The
77 Global Seismic Hazard Assessment Program (Giardini, 1999) also only published results for the
78 mean ground motion. The recent SHARE project (Giardini et al., 2013), which provides a
79 harmonized seismic hazard model for Europe, provides the results for the mean and various
80 fractiles and hence this study is selected as an example of a recent regional PSHA. This project
81 could be considered as following a SSHAC 2 philosophy. SSHAC refers to the Senior Seismic
82 Hazard Analysis Committee (Budnitz et al., 1997; USNRC, 2012), which sought to formalize the
83 procedures used to consider expert judgments within PSHAs, particularly those conducted for
84 critical infrastructure (e.g. nuclear power plants). It defined four types of study ranging from
85 Level 1, which corresponds to analyses conducted by a small team of analysts using publicly-
86 available information and without seeking outside expert advice, to Level 4, which corresponds
87 to a large-scale study with many participants with clearly defined roles and a highly formalized
88 procedure. Coppersmith and Bommer (2012) discuss the differences between these levels of

89 study. As the only two examples of PSHAs following the SSHAC Level 4 procedure to date, the
90 results of the Yucca Mountain (Stepp et al., 2001) and PEGASOS (NAGRA, 2004) projects are
91 included here. As examples of site-specific SSHAC Level 1, 2 and 3 studies some recent public
92 service and commercial projects of BRGM are included as well as recent studies for: a proposed
93 nuclear waste repository at Bruce (Canada), a planned nuclear power plant at Thyspunt (South
94 Africa), Cologne (Germany) and the Italian seismic building code. Brief summaries of the
95 selected studies are provided in Table 1 along with their SSHAC level; Figure 2 indicates the
96 locations of the European sites (the three non-European locations are not plotted).

97
98 Three metrics to measure the uncertainty in the expected IM [here either PGAs or PSA(1s)] for a
99 given AFE were originally considered: ratio of the 85th (or 84th) percentile IM (IM_{85}) and median
100 IM; ratio of median IM and 15th (or 16th) percentile (IM_{15}); and $100 \log(IM_{85}/IM_{15})$, which is
101 used by Giardini et al. (2004) in their report on the national Swiss hazard map (they call it the
102 relative uncertainty). When the distribution of the logarithm of the ground-motion level for a
103 given AFE is symmetrical about the median then these measures lead to the same conclusions.
104 This is not the case for asymmetric hazard distributions, such as those for Rome (INGV) where
105 the median is much closer (in logarithmic space) to the 85th percentile than the 15th, which are
106 due to the input parameters to the PSHA being skewed in logarithmic space. For simplicity and
107 since in most cases considered here the hazard distributions are roughly symmetric, we choose to
108 only report the third of these measures, i.e. $100 \log(IM_{85}/IM_{15})$.

109

110 **COMPARISONS**

111

112 In this section various hypotheses on observations that one would expect to see when examining
113 the uncertainties of hazard results are tested using the selected studies. A discussion of the
114 observations and their implications for PSHAs are given in the following section.

115

116 Firstly, because uncertainties should compound as return period increases (or AFE decreases) it
117 would be expected that the hazard curves for the different fractiles would spread out and the
118 uncertainty metric defined above would increase. This is checked by comparing the hazard
119 results for AFE=1/475 and AFE=1/2475 in the selected studies (Figures 3 and 4, compare gray
120 and black error bars from the same study). For the selected studies and AFEs the hazard results
121 do not always show this expected behavior: often the spread of fractiles is similar for 1/475 and
122 1/2475 and in some cases (e.g. for Gösgen from SHARE for PGA) the spread is much lower for
123 an AFE of 1/2475. A possible explanation for this apparent contradiction is that an uncertain
124 seismic source is dominant for higher AFEs but a better-known source becomes important as the
125 AFE decreases. Another possible reason (Julian Bommer, written communication, 2014) could be
126 that the dominant earthquakes for higher AFEs are smaller than for lower AFEs and predicted
127 IMs from small earthquakes ($M_w \sim 5$) show greater dispersion than for moderate magnitudes
128 ($M_w \sim 6.5$) (e.g. Douglas, 2010, compare his Figure 2 and 4).

129

130 Secondly, because the earthquake rate in stable areas is much lower (and consequently available
131 observations, both in terms of events and ground motions, fewer) than in active areas it would be
132 expected that the uncertainties in hazard estimates in those areas would be higher, provided that
133 similar rigor is applied to the assessment and capturing of uncertainties in the two cases. This is

134 checked by comparing the SHARE results for sites in the stable continental crust (the hazard,
135 according to SHARE, in the Scandinavian shield is lower and hence this regime is not considered
136 here) and active areas in Figures 3 and 4, using the seismotectonic zonation of Delavaud et al.
137 (2012, see Figure 2). As expected the uncertainties at sites in stable continental crust are much
138 higher than those in active areas. For the SHARE results this higher uncertainty in stable regions
139 is probably due in great part to the ground-motion logic tree branches, although the uncertainties
140 in the seismic source characterization are considerable. The ground-motion branches for stable
141 regions combined ground-motion models for active regions with models selected for the shield,
142 thereby leading to a large spread in the predicted ground motions for a given magnitude and
143 distance.

144
145 Thirdly, because the uncertainty in conducting hazard analyses for a large area (e.g. Europe or a
146 country) is higher than conducting it for a well-known site (e.g. a critical infrastructure) the logic
147 tree for the large area should, in theory, model a higher spread in the inputs than the logic tree for
148 the individual site. This is studied by comparing results for various sites from the national hazard
149 map for Italy, SHARE and some site-specific studies (Figures 3 and 4, compare results in section
150 ‘Differing geographical extents’). No systematic dependence on the geographical extent and the
151 uncertainty can be seen from this comparison. For some sites (e.g. Messina) the more local study
152 shows lower uncertainty than the analysis for the wider region (as expected), whereas for other
153 locations (e.g. Rome and Briançon for PGA) the uncertainty from the local study is higher than in
154 the PSHA for the broader region. This could be due to the local and national/regional study
155 making different levels of effort to capture the uncertainties in the seismic sources.
156 Computational limitations and time and resource constraints means that it is doubtful that studies
157 covering a large area could use the type of complex logic trees often developed and evaluated for

158 site-specific analyses. That being said, it may be possible to develop simple logic trees that
159 roughly capture the uncertainties in inputs to regional/national PSHAs so that the hazard fractiles
160 reflect, to a first-order, the uncertainties inherent in conducting such analyses. For a site-specific
161 study or low AFEs such simple logic trees, however, are unlikely to be appropriate.

162

163 Fourthly, because, as noted above, uncertainties in GMPEs appear to be only weakly dependent
164 on response spectral period it would be expected that the uncertainties in the PSHA would also
165 not show strong period dependency. This is examined by comparing Figure 3 (for PGA) and
166 Figure 4 [for PSA(1s)], and particularly by examining the ratios between the uncertainty
167 measures for PSA(1s) and PGA for each study (see right-most column on Figure 4). In general,
168 the uncertainties in the expected PSA(1s) values are slightly higher (ratios larger than unity) than
169 the spreads in the expected PGAs and in some cases (e.g. many of the SHARE results) much
170 higher (ratios of more than 1.5). These observations could be explained by, as noted above,
171 PSA(1s) being more sensitive to uncertainties in the recurrence rates of large earthquakes than
172 are PGAs. Based on disaggregation results, hazard for PSA(1s) often shows greater influence of
173 more distant sources than does PGA. Consequently, higher uncertainties at longer periods could
174 be due to consideration of more sources, the activity rates of which are poorly constrained. For
175 some sites and studies the uncertainties for PSA(1s) are lower than those for PGA. For Thyspunt
176 this can be attributed to large uncertainties in the estimates of the near-surface attenuation
177 (κ) at this site, which greatly affects the estimates of the short-period response spectral
178 accelerations but has no impact at 1s (Bommer et al., 2014, their Figure 15).

179

180 Finally, because of the rigorous approach of SSHAC 3 and 4 studies to fully capture uncertainties
181 in the seismic hazard it would be expected that expected ground motions from this level of study

182 would show a larger spread than results from SSHAC 1 and 2 projects. This is investigated by
183 comparing PEGASOS and SHARE results for four Swiss sites (Figures 3 and 4, compare results
184 in section ‘SSHAC 2, 3 and 4 studies’). From this figure it can be seen that hazard results from
185 PEGASOS (SSHAC 4) studies have wider fractiles than those from SHARE (SSHAC 2),
186 indicating higher uncertainties. Fractiles from the two SSHAC 4 studies (PEGASOS and Yucca
187 Mountain) and the SSHAC 3 study (Thyspunt) show similar spreads, as do the fractiles from the
188 SSHAC 2 study for Bruce. The AFEs of interest and purpose of SSHAC 3 and 4 studies should
189 be borne in mind when making this comparison. SSHAC 1 and 2 studies generally focus on
190 higher AFEs (1/2475 or higher) than SSHAC 3 and 4 studies (AFEs of 1/10000 and lower),
191 which are conducted for critical facilities that require high regulatory assurance that uncertainties
192 are correctly captured. Another observation that can be made is the large difference between the
193 median and mean IMs in the results from SSHAC 3 and 4 studies; for SHARE they are generally
194 similar. As noted by Abrahamson and Bommer (2005) the mean hazard curve is highly sensitive
195 to the most severe of the alternatives in the logic tree. SSHAC 3 and 4 studies often feature more
196 extreme alternatives in their logic trees and hence this drift across fractiles is more noticeable
197 than in SSHAC 1 and 2 results.

198

199 **DISCUSSION AND CONCLUSIONS**

200

201 The aim of state-of-the-art hazard assessments should be to account for the ‘center, body and
202 range of the technically defensible interpretations’ (USNRC, 2012) concerning inputs to the
203 analysis. For the ‘center’ the best-estimate model (e.g. the ground-motion model that is thought to
204 best represent the median ground motions in the region) or parameter (e.g. the best estimate for
205 the b value in the Gutenberg-Richter relation) should be used. The ‘body’ refers to the shape of

206 the alternative interpretations of the available data (e.g. accounting for the uncertainty in the *b*
207 estimate based on its standard deviation) and the ‘range’ refers to the tails of the interpretations
208 and limiting credible values (e.g. considering analogs to similar regions).

209
210 For the most-recent site-specific studies (e.g. the Thyspunt study by Bommer et al., 2014) this
211 objective appears to be reached but for national, regional or global studies this does not always
212 appear to be true. This is a question of the geographical scale at which the analysis is conducted:
213 at a small scale the activity of individual faults is considered and various source models may be
214 constructed whereas at a regional scale the uncertainties in sources may be neglected because
215 there is not the time to look at individual faults. However, the lack of knowledge in the regional-
216 scale source zonation should be considered. For the case of the SSHAC 3 and 4 studies
217 (PEGASOS, Yucca Mountain and Thyspunt), which show wide uncertainty ranges in Figure 3,
218 the hazard fractiles would have shown an even wider spread if the extensive data collection and
219 analyses (e.g. geological investigation of faults, investigations of historical seismicity and shear-
220 wave velocity measurements) conducted within these studies had not been made.

221
222 In the case of GMPEs, site-specific studies (e.g. Bommer et al., 2014) sometimes include
223 additional logic-tree branches to scale up or down a backbone GMPE to increase the spread in the
224 predicted ground motions (Bommer, 2012). This is done because it is believed that the sampling
225 of possible ground motions in the region is sparse and hence the average stress drop, for example,
226 is poorly known. This is not often done for hazard assessments of large zones (an exception is the
227 US National Hazard Maps). In the Global Earthquake Model’s (GEM) Global GMPEs project
228 there were only a few GMPEs selected per tectonic regime (Stewart et al., 2014) despite the large
229 uncertainty in predicting ground motions for all sites globally. It could have been better to

230 increase the spread in the logic tree by, for example, scaling up or down certain models, although
231 this scaling is currently difficult to calibrate, particularly for a project with a global scope such as
232 GEM.

233
234 Hazard assessments over large geographical regions (e.g. SHARE) require a harmonized
235 earthquake catalog, which often means that its lower magnitude limit is higher than for national
236 or site-specific study because of limited resources to compile, harmonize and analyze large
237 catalogs (the number of earthquakes roughly increases by ten times for every decrease by one
238 unit in the minimum magnitude). Consequently, the catalog compiled by SHARE only considers
239 events with $M_w > 3.5$, which for areas of low seismicity, in particular, means that the assessment
240 of the Gutenberg-Richter parameters is associated with lower precision (but not necessarily lower
241 accuracy) (Frank Scherbaum, written communication, 2014) than for national or site-specific
242 studies with catalogs that start at smaller magnitudes.

243
244 Recent PSHAs appear to have well characterized the center and often the body, since both can be
245 more readily quantified using available models and data, but the range does not appear to be fully
246 accounted for. This is because its assessment requires a quantification of what we do not know
247 rather than just what we do. For areas with limited data and knowledge (high uncertainty) the
248 body and range dominate the logic tree but these are more difficult to capture (and potentially
249 more subjective) whereas areas for which data are abundant the center is the most important. As
250 an example of this, the ground-motion logic trees used in SHARE (Delavaud et al., 2012) for
251 active shallow crustal areas has four models and two of which are assigned a total weight of 0.7,
252 whereas the logic tree for stable continental crust has five models all equally weighted. As
253 mentioned above, this demonstrates that the SHARE ground-motion expert group felt that the

254 uncertainty in the estimation of ground motions in stable continental crust is higher than in active
255 areas, which is understandable given the lack of strong-motion data from stable areas and the
256 relative abundance in active zones. Rather than simply considering the number and weights of the
257 selected GMPEs when comparing uncertainties in ground-motion logic trees it would be better to
258 measure the distribution of predicted ground motions using, for example, the composite ground-
259 motion model viewpoint (Scherbaum et al., 2005). For example, five GMPEs may be selected in
260 one study and two in another, which would give the impression that the first study accounted for
261 higher ground-motion uncertainty than the second, but if the five GMPEs all predicted similar
262 PGAs whereas the two from the other study predicted widely different motions then the second
263 study would actually model a higher uncertainty.

264
265 In order to more objectively capture uncertainty, the construction of logic trees for PSHA could
266 benefit from the application of innovative procedures to guide expert judgment. A purpose of
267 such methods would be to consolidate the assessments of a pool of experts. To merge all the
268 expert judgments, which occurs in a SSHAC Level 4 study, could possibly lead to
269 disproportionate spread in the integrated answer and, potentially, to some dubious results
270 (Aspinall, 2010). If a group of experts is gathered to get a synthesized position, social influence
271 could be magnified, e.g. the expert assessments could converge to the judgment of the most
272 renowned participant (Curtis, 2012), although in a properly-run SSHAC 3 or 4 study this should
273 not happen if the NUREG-2117 guidance is followed (USNRC, 2012). Runge et al. (2013)
274 present an approach to more rigorously assess expert weights for GMPEs within logic trees for
275 PSHA. The procedure is based on asking an expert a sequence of questions on his/her relative
276 confidence in one GMPE being more appropriate than another. A similar method could be

277 developed to assign weights to other parts of the logic tree, e.g. those concerning source activity
278 rates.

279
280 A standard step in SSHAC 3 and 4 studies is a sensitivity study examining the influence of the
281 different uncertainties on the hazard results. Such studies, often presented in the form of tornado
282 diagrams (e.g. Porter et al., 2012), allow the most important uncertainties to be identified. Based
283 on this information additional data collection or analysis may be undertaken in order to reduce
284 this lack of knowledge.

285
286 As a closing remark, we would like to encourage the publication of the uncertainties in hazard
287 studies because this makes studies more transparent and defensible to the wider community and it
288 would also help guide efforts to reduce the uncertainties. In addition, sensitivity studies on the
289 influence of the different uncertainties in the hazard results should be considered as a standard
290 requirement of all seismic hazard assessments. It should be the goal of all seismic hazard studies
291 to reduce the uncertainties as far as possible through collecting and analyzing data and
292 subsequently to characterize the remaining unknowns through the development of an appropriate
293 logic tree.

294
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398

<p>Sites, references; SSHAC level</p> <p>Brief description</p>
<p>Belfort (Rey et al., 2011), Lourdes (ISARD; Secanell et al., 2008) and Briançon (Le Goff et al., 2009); SSHAC Level 1</p> <p>These projects were supported by the French government, the European Interreg program or commercial clients, to assess hazard for various parts of France. They were conducted during a period of a few months by a small team based on data and knowledge available in the literature. The AFEs of interest were 1/2475 or greater.</p>
<p>Cologne (Grünthal and Wahlström, 2006); SSHAC Level 1</p> <p>This research study, conducted by a two-person team, computed the seismic hazard in a small area enclosing the cities of Cologne and Aachen (western Germany). It was part of a wider research project. The authors paid particular attention to accounting for uncertainties in the input parameters. The AFEs of interest were 1/2475 or greater.</p>
<p>Rome and Messina (INGV; Montaldo et al., 2007); SSHAC Level 2</p> <p>This large-scale project was conducted by INGV to produce the Italian seismic hazard map for use with a new building code. It involved inputs from many experts and included a review by a scientific board. The AFEs of interest were 1/2475 or greater.</p>
<p>Athens, Berlin, Beznau, Edinburgh, Gibraltar, Gösgen, Istanbul, Leibstadt, Mühleberg, Paris, Rome and Messina (SHARE; Giardini et al., 2013); SSHAC Level 2</p> <p>This three-and-a-half-year project, supported by the European Commission, produced a harmonized seismic hazard model for the wider European area. It involved 18 partner institutes and sought data and expertise from many dozens of experts outside the consortium, as well as being extensively reviewed. The AFEs of interest were 1/5000 or greater.</p>
<p>Bruce (AMEC Geomatrix, Inc., 2011); SSHAC Level 2</p> <p>This project assessed the seismic hazard at the site of a proposed deep geological repository for the permanent storage of low- and intermediate-level nuclear waste for Ontario Power Generation at Bruce (Municipality of Kincardine, Ontario, Canada). It involved correspondence with external experts to obtain unpublished data and an external review. The AFEs of interest ranged from 10^{-2} to 10^{-8}.</p>
<p>Thyspunt (Bommer et al., 2014); SSHAC Level 3</p> <p>This two-and-a-half-year project assessed the seismic hazard at the site of a proposed nuclear power plant in Eastern Cape (South Africa). It was the first application of the SSHAC 3 approach outside North America and involved many experts in a wide variety of roles. The AFEs of particular interest were 1/10000 and lower.</p>
<p>Beznau, Gösgen, Leibstadt, Mühleberg (PEGASOS; NAGRA, 2004); SSHAC Level 4</p> <p>This three-year project reassessed the seismic hazard at the four existing nuclear power plants in Switzerland. It was the second</p>

application of the SSHAC 4 approach. The AFEs of particular interest were 1/10000 and lower.

Yucca Mountain (CRWMS M&O; Stepp et al., 2001); SSHAC Level 4

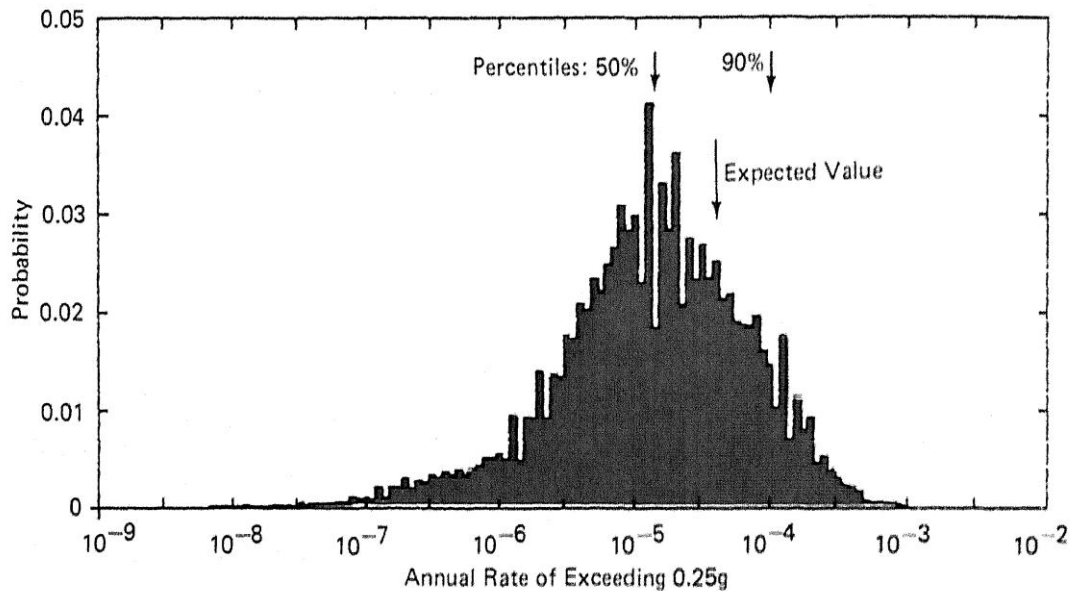
This four-year project assessed the seismic hazard for a planned nuclear waste repository beneath Yucca Mountain (Nevada). It was the first application of the SSHAC 4 process. The AFEs of particular interest were 1/10000 and lower.

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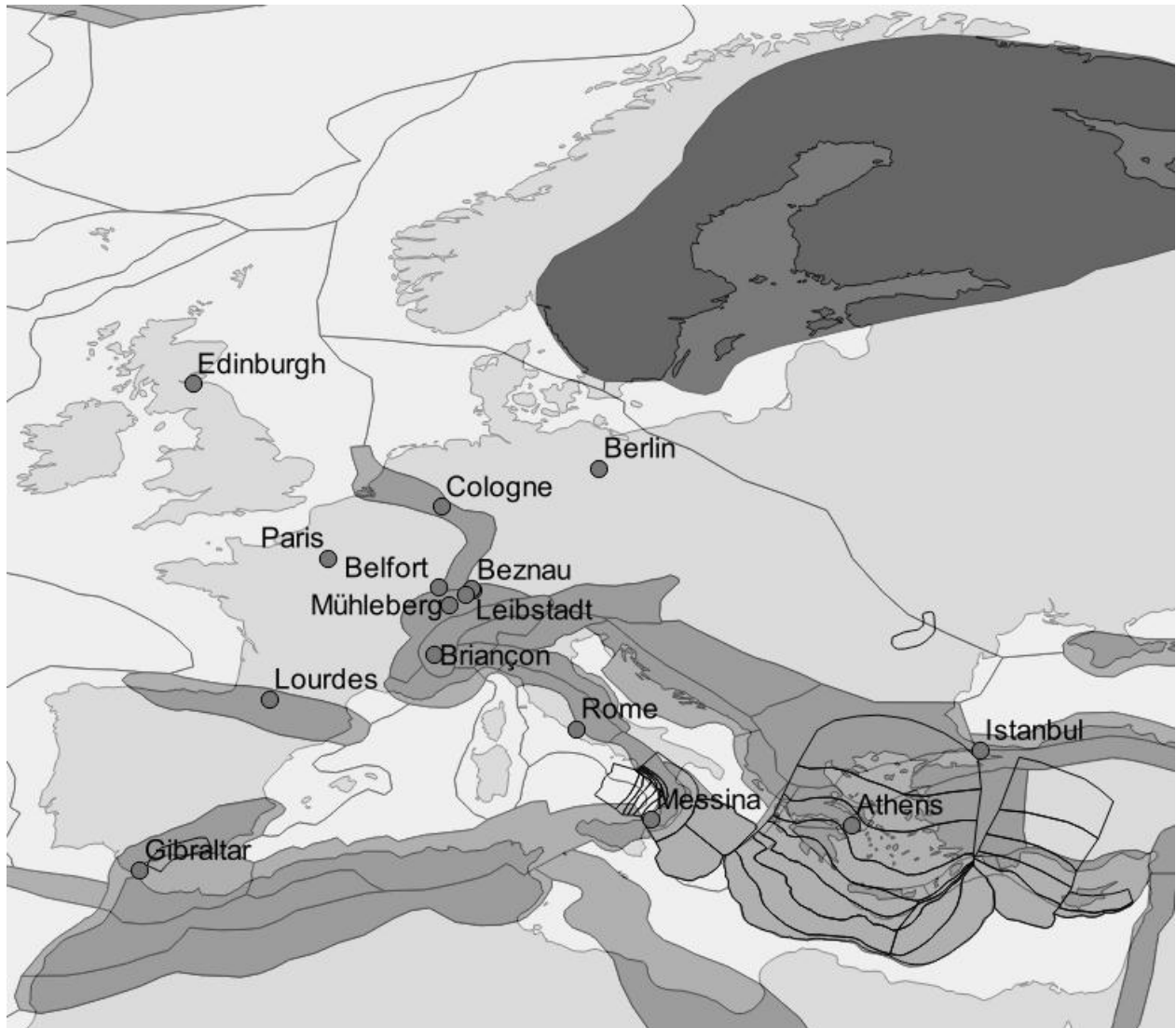
402 *Figures*

- 403 1. Example distribution of AFEs for a considered PGA of 0.25g for the WNP-2 nuclear power plant (Hanford
404 Reservation, Washington State) (Kulkarni et al., 1984, Reprinted with permission from EERI).
- 405 2. Locations of the selected sites in Europe (Bruce, Canada; Thyspunt, South Africa; and Yucca Mountain,
406 Nevada, are outside the map) overlying the subdivisions of the Euro-Mediterranean area into its main
407 tectonic regimes developed for the SHARE project (Delavaud et al., 2012) where: dark gray indicates
408 shield; mid-gray active areas; light gray stable continental crust and black lines: subduction zones and areas
409 of deep-focus non-subduction earthquakes (Vrancea).
- 410 3. Comparison of expected PGAs [AFE of 1/475 (black) and 1/2475 (gray) return periods] from different
411 PSHAs (bars indicate 15th -85th fractiles, crosses the medians and squares the means) and the uncertainty
412 metric $100 \log(\text{PGA}_{85}/\text{PGA}_{15})$. It should be noted that for Thyspunt (indicated by an asterisk), a low-kappa
413 site, that PGA corresponds to spectral acceleration at a frequency greater than 100Hz (not computed in the
414 study) and the results for a pseudo-spectral accelerations for 100Hz are plotted here (Bommer et al., 2014).
415 The studies are split vertically to help comparisons discussed in the text. Note that estimates of the mean
416 PGAs are not available for Rome (INGV), Messina (INGV), Briançon (BRGM) and Lourdes (ISARD),
417 which also does not provide ground-motion estimates for AFE of 1/2475.
- 418 4. Comparison of expected PSA(1s) [AFE of 1/475 (black) and 1/2475 (gray) return periods] from different
419 PSHAs (bars indicate 15th -85th fractiles, crosses the medians and squares the means), the uncertainty metric
420 $100 \log(\text{PSA}_{85}/\text{PSA}_{15})$ and the ratio of the uncertainty metrics for PSA(1s) and PGA (ratios lower than 0.5
421 or higher than 1.5 are indicated in bold). The studies are split vertically to help comparisons discussed in the
422 text. Note that estimates of the mean PSAs(1s) are not available for: Rome (INGV), Messina (INGV),
423 Briançon (BRGM) and Lourdes (ISARD), which also does not provide ground-motion estimates for a return
424 period of 2475 years; the expected PSA(1s) for an AFE of 1/475 for the four PEGASOS sites are not
425 available for the considered fractiles.



426

427 **Figure 1.** Example distribution of AFEs for a considered PGA of 0.25g for the WNP-2 nuclear power
 428 plant (Hanford Reservation, Washington State) (Kulkarni et al., 1984, Reprinted with permission from
 429 EERI).



430
 431 **Figure 2.** Locations of the selected sites in Europe (Bruce, Canada; Thyspunt, South Africa; and Yucca
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 435 zones and areas of deep-focus non-subduction earthquakes (Vrancea).

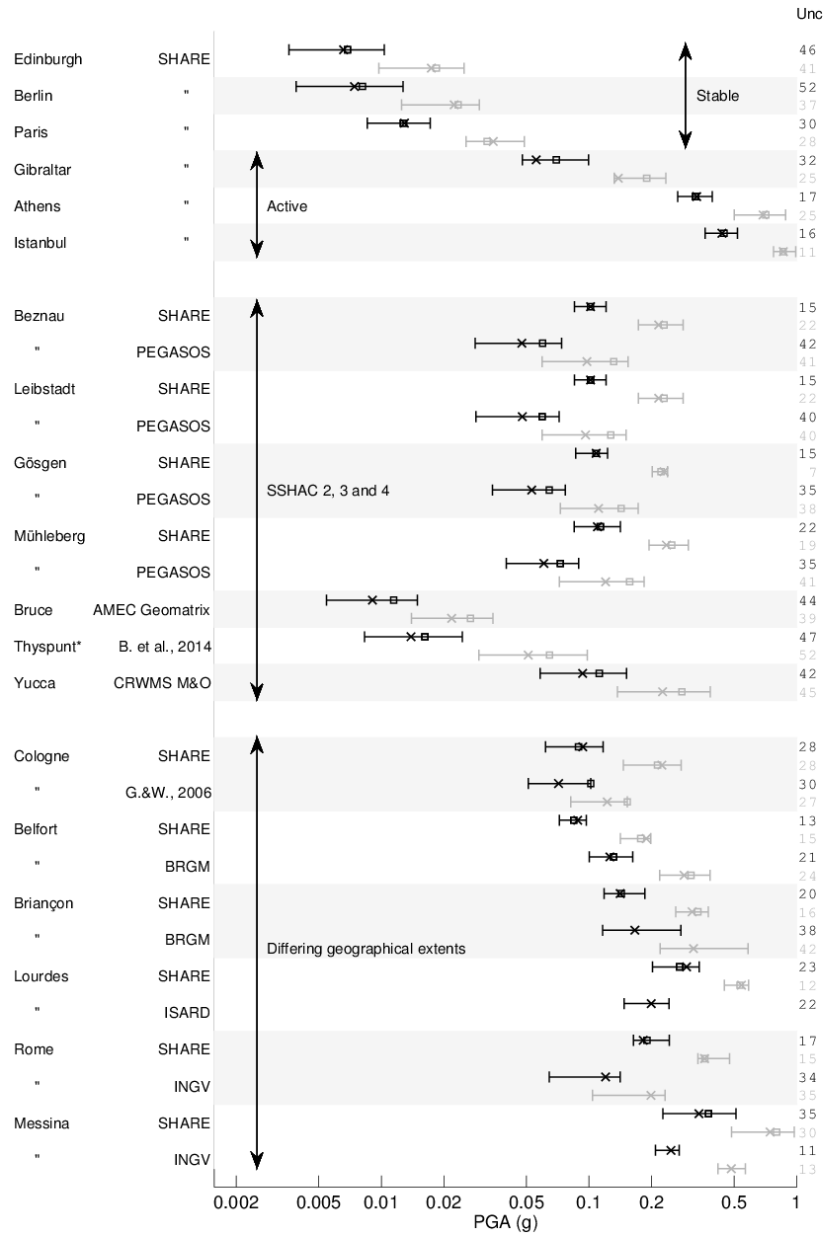


Figure 3. Comparison of expected PGAs [AFE of 1/475 (black) and 1/2475 (gray) return periods] from different PSHAs (bars indicate 15th -85th fractiles, crosses the medians and squares the means) and the uncertainty metric $100 \log(PGA_{85}/PGA_{15})$. It should be noted that for Thyspunt (indicated by an asterisk), a low-kappa site, that PGA corresponds to spectral acceleration at a frequency greater than 100Hz (not computed in the study) and the results for a pseudo-spectral accelerations for 100Hz are plotted here (Bommer et al., 2014). The studies are split vertically to help comparisons discussed in the text. Note that estimates of the mean PGAs are not available for Rome (INGV), Messina (INGV), Briançon (BRGM) and Lourdes (ISARD), which also does not provide ground-motion estimates for AFE of 1/2475.

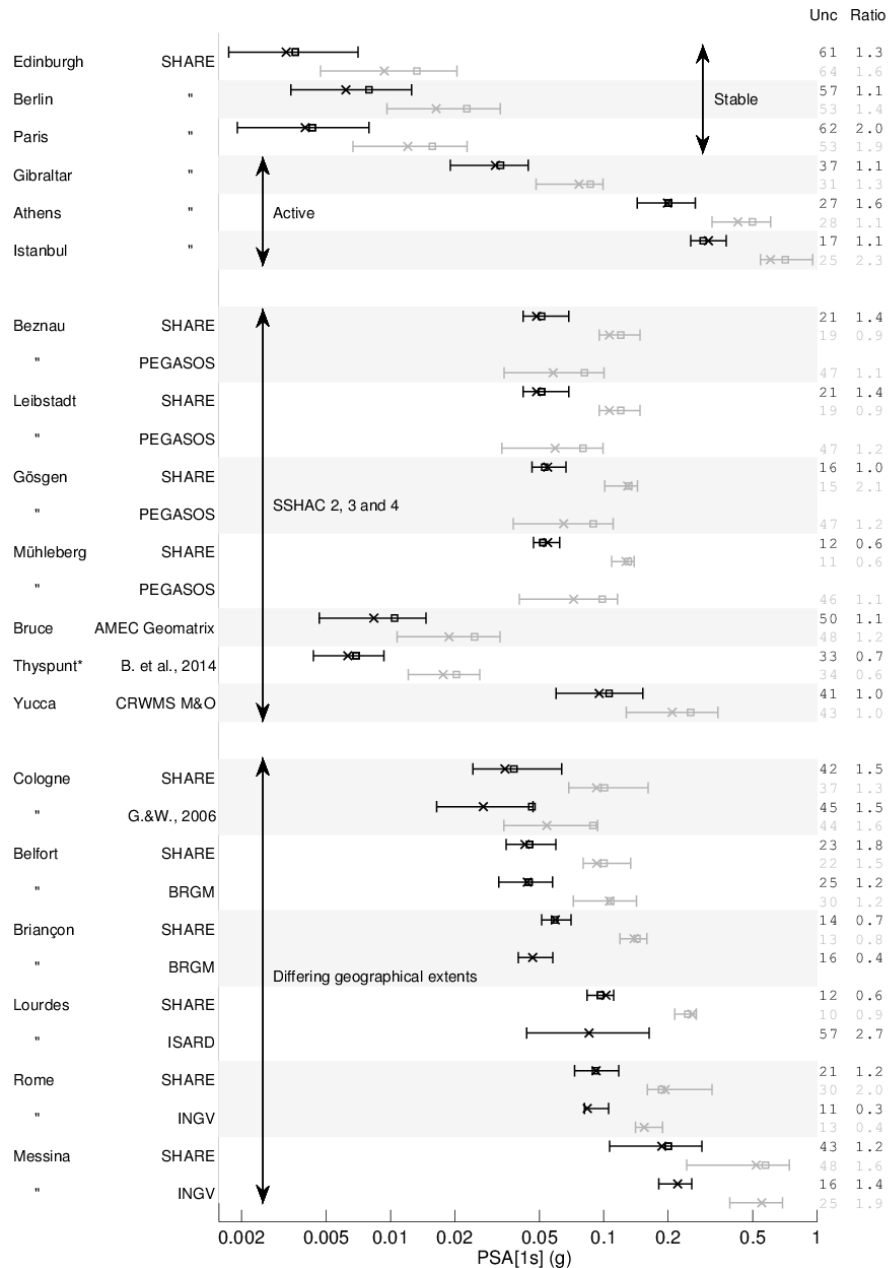


Figure 4. Comparison of expected PSA(1s) [AFEs of 1/475 (black) and 1/2475 (gray) return periods] from different PSHAs (bars indicate 15th -85th fractiles, crosses the medians and squares the means), the uncertainty metric $100 \log(\text{PSA}_{85}/\text{PSA}_{15})$ and the ratio of the uncertainty metrics for PSA(1s) and PGA (ratios lower than 0.5 or higher than 1.5 are indicated in bold). The studies are split vertically to help comparisons discussed in the text. Note that estimates of the mean PSAs(1s) are not available for: Rome (INGV), Messina (INGV), Briançon (BRGM) and Lourdes (ISARD), which also does not provide ground-motion estimates for a return period of 2475 years; the expected PSA(1s) for an AFE of 1/475 for the four PEGASOS sites are not available for the considered fractiles.